**Instructions:** No notes or calculators are allowed. Answers must be supported by work on your exam sheets. Answers with little or no supporting work will receive little or no credit. **Work must be neat, organized and easily interpreted.** Simplify all answers unless otherwise indicated. Please circle your final answers.

## Practice 1

- 1. (15 pts) For the function  $f(x) = 3x^2$ , find a formula for a Riemann sum obtained by dividing the interval [0, 1] into *n* equal subintervals and using the RIGHT-hand endpoint for each  $c_k$ . Then take a limit of these sums as  $n \to \infty$  to calculate the area under the curve over [0, 1].
- 2. (5 pts) Express the limit  $\lim_{\|P\|\to 0} \sum_{k=1}^{n} c_k^5 \Delta x_k$ , *P* a partition of [8,11], as a definite integral.
- 3. Use the Fundamental Theorem of Calculus to:
  - a. (5 pts) Find  $\frac{dy}{dx}$  for  $y = \int_0^x \sqrt{5 + 6t^2} dt$ . b. (5 pts) Find  $\frac{dy}{dx}$  for  $y = \int_0^{x^2} \sqrt{5 + 6t^2} dt$  [hint: also use the Chain Rule].
- 4. Integrate the following indefinite integrals.

a. (8 pts) 
$$\int x^{1/3} \sin(x^{4/3} + 8) dx$$
  
b. (7 pts)  $\int \frac{t^3 - t^{5/2}}{t^2} dt$ 

c. (8 pts) 
$$\int 3y^5 \sqrt{y^3 + 1} \, dy$$

- d. (7 pts)  $\int \tan^2 \theta \sec^2 \theta \, d\theta$
- 5. Determine the values of the following definite integrals.
  - a. (10 pts)  $\int_0^1 \frac{e^x}{1+e^x} dx$ b. (10 pts)  $\int_0^{\pi/6} \cos^{-3} 2t \sin 2t dt$

c. (10 pts) 
$$\int_{-1}^{1} \theta^3 (1+\theta^4)^3 d\theta$$

6. (10 pts) Find the area of the region enclosed by the curves  $9x^2 + y = 9$  and  $x^4 - y = 1$ .

**BONUS PROBLEM** (8 pts) Evaluate **JUST ONE** of the following definite integrals. If you try both, you must neatly cross out the one you do not want graded, otherwise **neither** problem will receive credit.

A. 
$$\int_{0}^{4/3} \frac{3}{16+9r^2} dr$$
  
B.  $\int_{e}^{e^2} \frac{2}{z \ln(z)} dz$ 

## Practice 2

- 1. (10 pts) Use the Midpoint Rule to estimate the area under  $y = \frac{5}{x}$  over the interval [1, 25] using six rectangles of equal width. Do not simplify your answer.
- 2. (5 pts) Express the limit  $\lim_{\|P\|\to 0} \sum_{k=1}^{n} c_k^9 \Delta x_k$ , *P* a partition of [3, 5], as a definite integral.
- 3. Use the Fundamental Theorem of Calculus to:

a. (5 pts) Find 
$$\frac{dy}{dx}$$
 for  $y = \int_0^x \sqrt{3 + 4t^2} dt$ .  
b. (5 pts) Find  $\frac{dy}{dx}$  for  $y = \int_0^{\tan x} \sqrt{3 + 4t^2} dt$  [hint: also use the Chain Rule].

- 4. Integrate the following indefinite integrals.
  - a.  $(10 \text{ pts}) \int (2\theta + 1 + 2\cos(2\theta + 1)) d\theta$ b.  $(10 \text{ pts}) \int \frac{(t+1)^2 - 1}{t^4} dt$ c.  $(10 \text{ pts}) \int \frac{(\ln y)^{-3}}{v} dy$
- 5. Determine the values of the following definite integrals.

a. (15 pts) 
$$\int_{-\pi/3}^{0} \sec x \tan x \, dx$$

b. (15 pts) 
$$\int_0^{\ln 5} e^r (3e^r + 1)^{-3/2} dr$$

6. (15 pts) Find the total area of the shaded regions.



**BONUS PROBLEM** (8 pts) Evaluate **JUST ONE** of the following definite integrals. If you try both, you must neatly cross out the one you do not want graded, otherwise **neither** problem will receive credit.

A. 
$$\int_{-2}^{2} \frac{3}{4+3t^{2}} dt$$
  
B.  $\int_{\sqrt{3}}^{\sqrt{8}} z^{3}\sqrt{z^{2}+1} dz$ 

## Practice 3

- 1. (10 pts) Use the Midpoint Rule to estimate the area under  $y = \frac{3}{x^2}$  over the interval [2, 22] using five rectangles of equal width. **Do not simplify your answer.**
- 2. (5 pts) Express the limit  $\lim_{\|P\|\to 0} \sum_{k=1}^{n} c_k^3 \Delta x_k$ , *P* a partition of [2,8], as a definite integral.
- 3. Use the Fundamental Theorem of Calculus to:

a. (5 pts) Find 
$$\frac{dy}{dx}$$
 for  $y = \int_0^x \sqrt{5 + 17t^3} dt$ .  
b. (5 pts) Find  $\frac{dy}{dx}$  for  $y = \int_0^{\ln x} \sqrt{5 + 17t^3} dt$  [hint: also use the Chain Rule].

4. Integrate the following indefinite integrals.

a. (10 pts) 
$$\int \left(\frac{1}{\sqrt{2\theta - \pi}} + 2 \sec^2(2\theta - \pi)\right) d\theta$$
  
b. (10 pts)  $\int \left(t - \frac{2}{t}\right) \left(t + \frac{2}{t}\right) dt$   
c. (10 pts)  $\int \frac{\cos(\ln y)}{y} dy$ 

5. Determine the values of the following definite integrals.

a. (15 pts) 
$$\int_{-\pi/6}^{0} \sec x \tan x \, dx$$
  
b. (15 pts)  $\int_{0}^{\ln 10} e^{r} (e^{r} - 1)^{1/2} \, dr$ 

6. (15 pts) Find the total area of the shaded regions.



**BONUS PROBLEM** (8 pts) Evaluate **JUST ONE** of the following definite integrals. If you try both, you must neatly cross out the one you do not want graded, otherwise **neither** problem will receive credit.

A. 
$$\int_{2/3}^{2\sqrt{3}/3} \frac{3}{4+3t^2} dt$$
  
B.  $\int_{-1}^{0} 3z^5 \sqrt{z^3 + 1} dz$