

CHAPTER 4

$$4.1 \quad P_r = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 d^2} = \frac{(1/3)^2 (10)(1)(1)}{(4\pi)^2 (1000)^2} = 7.036 \cdot 10^{-9} \text{ W}$$

$$4.2 \quad a) \quad P_r = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 d^2} = \frac{(50)(1)(1)(1/20)^2}{(4\pi)^2 (10^4)^2} = 7.910 \cdot 10^{-12} \text{ W}$$

$$b) \quad P_r = P_d \cdot A_e = \left[\frac{|E|^2}{120\pi} \right] \cdot A_e = \frac{|E|^2}{120\pi} \cdot \frac{G_r \lambda^2}{4\pi}$$

$$A_e = \frac{G \lambda^2}{4\pi}$$

$$E = P_r \cdot (120\pi)(4\pi) / \lambda^2 G_r = 3.9 \times 10^{-3} \text{ V/m}$$

$$c) \quad P_r = \frac{\left[\frac{V_{\text{ant}}}{2} \right]^2}{50 \Omega} \Rightarrow \sqrt{7.910 \cdot 10^{-12} \cdot 50 \cdot 4} = V_{\text{ant}} \quad \text{open circuit}$$

$$V_{\text{ant}} = 4 \cdot 10^{-5} \text{ Volts rms} \quad \text{open circuit}$$

$$V_{\text{rcvr}} = \frac{V_{\text{ant}}}{2} = 2 \cdot 10^{-5} \text{ Volts rms}$$

4.3 Fraunhofer Distance:

$$a = 4.6 \text{ cm} \quad (2)$$

$$b = 3.5 \text{ cm} \quad (3)$$

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8}{60 \times 10^9} = 0.005 \text{ m} \quad (4)$$

In azimuth:

$$HPBW = \frac{51\lambda}{b} = \frac{51 \times 0.005}{0.035} = 7.3^\circ \quad (5)$$

In elevation:

$$HPBW = \frac{51\lambda}{a} = \frac{51 \times 0.005}{0.046} = 5.5^\circ \quad (6)$$

$$G = \frac{4\pi A_e}{\lambda^2} = \frac{4\pi ab}{\lambda^2} = 29 \text{ dB} \quad (7)$$

$$D = \sqrt{a^2 + b^2} = 5.78 \text{ cm} \quad (8)$$

$$D_f = \frac{2D^2}{\lambda} = \frac{2 \times 0.0578^2}{0.005} = 1.34 \text{ m} \quad (9)$$